# Reaction of Dehydrated $\mathrm{Na}_{12}-$ A with Cesium. Synthesis and Crystal Structure of Fully Dehydrated, Fully $\mathrm{Cs}^{+}$-Exchanged Zeolite A 

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#### Abstract

A most ionically crowded zeolite, fully dehydrated, fully $\mathrm{Cs}^{+}$-exchanged zeolite A , has been synthesized by the reduction of all $\mathrm{Na}^{+}$ions in $\mathrm{Na}_{12}-\mathrm{A}$ by cesium vapor. The redox reaction goes to completion at $350^{\circ} \mathrm{C}$ with 0.1 Torr of $\mathrm{Cs}^{0}$ to give $\mathrm{Cs}_{12}-\mathrm{A} \cdot \cdot^{1} / 2 \mathrm{Cs}$; an intermediate composition $\mathrm{Cs}_{8.5} \mathrm{Na}_{3.5}-\mathrm{A} \cdot 1 / 2 \mathrm{Cs}$ formed upon reaction at $250^{\circ} \mathrm{C}$. Two crystal structures of $\mathrm{Cs}_{12}-\mathrm{A}^{1} / 2 \mathrm{Cs}(a=12.279$ and $12.276 \AA)$ and one of $\mathrm{Cs}_{8.5} \mathrm{Na}_{3.5}-\mathrm{A} \cdot 1 / 2 \mathrm{Cs}(a=12.252 \AA)$ have been determined by single-crystal X-ray diffraction methods in the cubic space group $P m 3 m$ with final $R$ (weighted) indices of $0.042,0.042$, and 0.052 , respectively. $\mathrm{Cs}_{12}-\mathrm{A} \cdot{ }^{1} / 2 \mathrm{Cs}$ may be viewed as a mixture of $\mathrm{Cs}_{12}-\mathrm{A}$ and $\mathrm{Cs}_{12}-\mathrm{A} \cdot \mathrm{Cs}$, and $\mathrm{Cs}_{8.5} \mathrm{Na}_{3.5}-\mathrm{A} \cdot{ }^{1 / 2} \mathrm{Cs}$, as a mixture of $\mathrm{Cs}_{8} \mathrm{Na}_{4}-\mathrm{A}$ and $\mathrm{Cs}_{9} \mathrm{Na}_{3}-\mathrm{A} \cdot \mathrm{Cs}$. In each of these, three $\mathrm{Cs}^{+}$ions are located at the centers of 8 -rings and two $\mathrm{Cs}^{+}$ions are found in the sodalite unit (except $\mathrm{Cs}_{8} \mathrm{Na}_{4}-\mathrm{A}$, which has only one). In $\mathrm{Cs}_{12}-\mathrm{A}$ and $\mathrm{Cs}_{12}-\mathrm{A} \cdot \mathrm{Cs}$, six and eight $\mathrm{Cs}^{+}$ions per unit cell, respectively, lie opposite 6 -rings in the large cavity. In $\mathrm{Cs}_{8} \mathrm{Na}_{4}-\mathrm{A}$ and $\mathrm{Cs}_{9} \mathrm{Na}_{3}-\mathrm{A} \cdot \mathrm{Cs}$, the unreacted $\mathrm{Na}^{+}$ions remain nearly on 6 -ring planes and four $\mathrm{Cs}^{+}$ions are found on threefold axes deep in the large cavity, $3.00 \AA$ from $\mathrm{O}(3)$ oxygens. One $\mathrm{Cs}^{+}$ion in $\mathrm{Cs}_{12}-\mathrm{A}$ and one in $\mathrm{Cs}_{8} \mathrm{Na}_{4}-\mathrm{A}$ are found in the large cavity near a 4 -ring that is adjacent to two 6 -rings; these 6 -rings are occupied by two sodalite-unit $\mathrm{Cs}^{+}$ions in $\mathrm{Cs}_{12}-\mathrm{A}$ and by such a $\mathrm{Cs}^{+}$ion and a $\mathrm{Na}^{+}$ion in $\mathrm{Cs}_{8} \mathrm{Na}_{4}-\mathrm{A}$. In each structure, 0.5 excess cesium was found per unit cell. The zeolite appears to be able to decrease the net electrostatic repulsive energy among its crowded cesium ions and to form some weak metal-metal bonds, by sorbing extra Cs atoms. $\mathrm{Cs}_{12}-\mathrm{A} \cdot 1 /{ }_{2} \mathrm{Cs}$ and $\mathrm{Cs}_{8.5} \mathrm{Na}_{3.5}-\mathrm{A} \cdot 1 /{ }_{2} \mathrm{Cs}$ may be viewed as materials with 12.5 ions and 0.5 excess electron per unit cell. Each extra Cs atom associates with three $\mathrm{Cs}^{+}$ions to form a linear $\left(\mathrm{Cs}_{4}\right)^{3+}$ cluster, which lies on a threefold axis and extends through the center of the sodalite unit. If the zeolite framework is silicon-rich, $\left(\mathrm{Cs}_{2}\right)^{+}$would be present in sodalite units of composition $\mathrm{Cs}_{11} \mathrm{Si}_{13} \mathrm{Al}_{11} \mathrm{O}_{48}$. Cs .


Fully dehydrated, fully $\mathrm{Cs}^{+}$-exchanged zeolite A , if it could be prepared, would be a most ionically crowded zeolite. The arrangement that 12 such large ions $\left(r_{\mathrm{Cs}^{+}}=1.67 \AA\right)^{1}$ would adopt in a $12.3-\AA$ unit cell was difficult even to anticipate and would necessarily be novel. Surely the large $\mathrm{Cs}^{+}$ions must remain more distant from the inner surfaces of the zeolite than smaller ions and therefore closer to the centers of the cavities and to each other. The unusually short approaches that must occur, unless they are destabilizing enough to prevent the formation of $\mathrm{Cs}_{12}-\mathrm{A}$, might impart some interesting properties to this material.

Beginning in 1956, Breck et al. reported that cesium ion exchange into zeolite A with a $100 \%$ excess of $\mathrm{Cs}^{+}(0.14 \mathrm{M}$ aqueous solution at $90^{\circ} \mathrm{C}$ ) resulted in the replacement of only $31 \%$ of the $\mathrm{Na}^{+}$ions in the structure. ${ }^{2}$ Later Barrer et al. increased the level of $\mathrm{Cs}^{+}$exchange to $45 \%$ by exposing the zeolite to succesive concentrated aqueous solutions at $25^{\circ} \mathrm{C} .{ }^{3}$ When "adjusted to a standard equilibrium solution strength" of 0.1 M , the level of $\mathrm{Cs}^{+}$exchange was calculated to be about $60 \%$, about $7 / 12 .{ }^{3.4} \mathrm{~A}$ number of attempts made in this laboratory to accomplish full $\mathrm{Cs}^{+}$exchange into zeolite A by various ion-exchange strategies have allowed the maximum extent of $\mathrm{Cs}^{+}$exchange to increase gradually during the past decade from $7 / 12$ to $11 / 12 .{ }^{5-10}$

By straightforward exhaustive methods of exchange (an aqueous $\mathrm{Cs}^{+}$solution flowed past a single crystal in a capillary), $\mathrm{Cs}_{7} \mathrm{Na}_{5}-\mathrm{A},{ }^{5}$ $\mathrm{Cs}_{7} \mathrm{~K}_{5}-\mathrm{A},{ }^{6}$ and $\mathrm{Cs}_{9} \mathrm{Tl}_{3}-\mathrm{A}^{7}$ were prepared. It was surprising initially to see these apparent ion-exchange limits. Methods involving the chemical complexation of the leaving cation led to $\mathrm{Cs}_{7,3^{-}}$

[^0]$\mathrm{Ag}_{4.7}-\mathrm{A}^{8}$ and $\mathrm{Cs}_{8.5} \mathrm{Ag}_{3.5}$-A. ${ }^{9}$ Even though there appeared to be no fundamental reason why full $\mathrm{Cs}^{+}$exchange could not be achieved, the conventional ion-exchange methods, which rely only on the principle of mass action and complexation, were clearly inadequate. This could not be explained by ion sieving ${ }^{4}$ because one $\mathrm{Cs}^{+}$ion was always found inside each sodalite unit in all of the partially $\mathrm{Cs}^{+}$-exchanged structures studied. ${ }^{5-10}$ Furthermore, the crystal structures clearly demonstrated that exchange limits occurred at compositions where intercationic distances can all remain greater than some limiting value: replacing one more smaller cation with $\mathrm{Cs}^{+}$would generate some new substantially shorter $\mathrm{Cs}^{+}-\mathrm{Cs}^{+}$contacts. One may surmise that the energy barriers that effectively prevent complete $\mathrm{Cs}^{+}$exchange are due to ion crowding.

It was only recently that 10 or more $\mathrm{Cs}^{+}$ions per unit cell were exchanged into zeolite $\mathrm{A}^{10}$ This involved methods that annihilate the leaving cation, $\mathrm{NH}_{4}^{+}$, by reaction with $\mathrm{OH}^{-}$and resulted in the preparation of $\mathrm{Cs}_{10} \mathrm{Na}_{4}(\mathrm{OH})_{2}-\mathrm{A}$ and $\mathrm{Cs}_{11} \mathrm{X}_{2}\left(\mathrm{H}_{3} \mathrm{O}\right)(\mathrm{OH})_{2}-\mathrm{A}$ ( $\mathrm{X}=$ an alkali-metal cation), in which hydroxide ions bridge between the closest $\mathrm{Cs}^{+}$ions. These hydroxide ions stabilize the high concentration of $\mathrm{Cs}^{+}$ions in the cavities of zeolite A , and they are retained even though additional alkali-metal cations must concomitantly remain with the zeolite. This is similar to salt imbibation ${ }^{11}$ and can be viewed as overexchange. ${ }^{12,13}$

More recently, the reaction of hydrated $\left(\mathrm{NH}_{4}{ }^{+}\right)_{12}-\mathrm{A}$ with cesium hydroxide successfully produced $\mathrm{Cs}_{12}-\mathrm{A} \cdot \mathrm{CsOH},{ }^{14}$ zeolite A containing no exchangeable cations other than $\mathrm{Cs}^{+}$but with one extra molecule of cesium hydroxide per unit cell. This hydroxide ion could not be identified crystallographically (the data set was small) but is likely to be located between the two cesium ions in the sodalite unit. An attempt to remove the extra CsOH by heating $\mathrm{Cs}_{12}-\mathrm{A} \cdot \mathrm{CsOH}$ at $350^{\circ} \mathrm{C}$ was unsuccessful, probably

[^1]because the hot cesium hydroxide was corrosive to the zeolite framework.

This work was initiated with the hope that the intrazeolitic redox potential for the reaction

$$
\mathrm{Na}_{12}-\mathrm{A}+12 \mathrm{Cs}^{0} \rightarrow \mathrm{Cs}_{12}-\mathrm{A}+12 \mathrm{Na}^{0}
$$

would be positive enough to provide an important additional driving force toward complete exchange. The following $\Delta E$ values, not involving the zeolite, are readily calculated. ${ }^{15}$

$$
\begin{gathered}
\mathrm{Cs}(\mathrm{~s})+\mathrm{Na}^{+} \rightarrow \mathrm{Cs}^{+}+\mathrm{Na}(\mathrm{~s}) \quad \Delta E_{\mathrm{aq}}^{\circ}=+0.21 \mathrm{~V} \\
\mathrm{Cs}(\mathrm{~g})+\mathrm{Na}^{+} \rightarrow \mathrm{Cs}^{+}+\mathrm{Na}(\mathrm{~g}) \quad \Delta E_{\mathrm{aq}}\left(25^{\circ} \mathrm{C}\right)=+0.41 \mathrm{~V}
\end{gathered}
$$

The $\Delta E$ value for the latter reaction was calculated with vapor pressures of $1.0 \times 10^{-1}$ Torr for pure $\mathrm{Cs}^{0}$ at $209^{\circ} \mathrm{C}$ and $2.3 \times$ $10^{-8}$ Torr for $\mathrm{Na}^{0}$ at the same temperature. (Its mole fraction in the $\mathrm{Cs}(\mathrm{l})$ should be very small and was approximated to be $1.0 \times 10^{-4}$ by considering the amounts of $\mathrm{Cs}^{0}$ used and $\mathrm{Na}^{0}$ produced by reaction with only one crystal of $\mathrm{Na}_{12}-\mathrm{A}$.) Calculations to correct this value to actual crystal reaction temperatures have not been done; one may assume that the changes would be small because the heat capacities of the reactants are comparable to those of the products. All reduced sodium atoms should have migrated out of the zeolite lattice and should have distilled away from the crystal's surface, so that a crystal, e.g. at $350^{\circ} \mathrm{C}$, would indeed be in contact with only $\mathrm{Cs}(\mathrm{g})$ and $\mathrm{Na}(\mathrm{g})$.

This reaction may be viewed as a way of achieving ion exchange without the use of a solvent. If successful, such redox methods of ion exchange might generally allow problems of hydrolysis and overexchange to be circumvented. These problems are often encountered when ion exchange from aqueous solution is attempted.

## Experimental Section

Colorless crystals of zeolite 4 A (stoichiometry $\mathrm{Na}_{12} \mathrm{Si}_{12} \mathrm{Al}_{12} \mathrm{O}_{48}$. $27 \mathrm{H}_{2} \mathrm{O}$; a composition near this with $\mathrm{Si} / \mathrm{Al}$ ca. 1.04 has been proposed) were prepared by Charnell's method. ${ }^{16}$ A single crystal, a cube 0.08 mm on an edge, was lodged in a fine Pyrex capillary on a vacuum line. After complete dehydration at $350^{\circ} \mathrm{C}\left(1 \times 10^{-5}\right.$ Torr) for 2 days, ${ }^{17}$ cesium vapor ( $99.98 \%$ purity; Johnson Matthey Inc.) was introduced by distillation from a side-arm break-seal ampule to the glass-tube extension of the crystal-containing capillary. This glass reaction vessel was then sealed off under vacuum and placed within two cylindrical coaxially attached horizontal ovens. The oven about the crystal was always maintained at a higher temperature than that about the cesium metal so that cesium would not distill onto the crystal.

The first reaction, carried out at $250^{\circ} \mathrm{C}$ (ca. 0.1 Torr of cesium vapor) (cesium source at $200^{\circ} \mathrm{C}^{18}$ ) for 16 h , resulted in incomplete reaction (crystal 1). A second crystal of $\mathrm{Na}_{12}-\mathrm{A}$ was prepared similarly and allowed to react at a higher temperture, $350^{\circ} \mathrm{C}$ (ca. 0.1 Torr of cesium vapor), for 16 h (crystal 2). The resulting black crystals were sealed off from the reaction vessel by torch after cooling to room temperature. A third crystal (crystal 3) was prepared as crystal 2 was but was then heated at $450^{\circ} \mathrm{C}\left(1 \times 10^{-5}\right.$ Torr) for 4 days to ensure that all of the reduced sodium metal had distilled from its surface. The true color of the crystal could certainly then be seen under the microscope; like crystals 1 and 2, it was black and lusterous.
A Syntex four-circle computer-controlled diffractometer with a graphite monochromator and a pulse-height analyzer was used for preliminary experiments and for the subsequent collection of diffraction intensities, all at $24(1)^{\circ} \mathrm{C}$. Molybdenum radiation ( $\mathrm{K} \alpha_{1}, \lambda=0.70930$ $\AA ; K \alpha_{2}, \lambda=0.71359 \AA$ ) was used throughout.

Diffraction data for the " b " reflections of the $F m 3 c$ superstructure of crystal 3 were carefully examined at a scan rate of $0.25^{\circ} \mathrm{min}^{-1}$ with a scan/background time ratio of 1.0 in the range of $2^{\circ} \leq 2 \theta \leq 25^{\circ}$. Only one reflection $(1,3,5)$ had an intensity above its $3 \sigma$ level. This indicates substantially less b reflection intensity than is usually observed for zeolite A. ${ }^{19}$ For this reason, as well as for others discussed previously, ${ }^{20,21} \mathrm{Pm} 3 \mathrm{~m}$

[^2]was used instead of $F m 3 c$ throughout this work.
In each case, the cell constant, $a=12.252$ (1), 12.279 (1), and 12.276 (1) $\AA$ for crystals $1-3$, respectively, was determined by a least-squares treatment of 15 intense reflections for which $18^{\circ}<2 \theta<30^{\circ}$. The $\theta-2 \theta$ scan technique was used for data collection. Each reflection was scanned at a constant rate of $1.0^{\circ} \mathrm{min}^{-1}$ from $1^{\circ}$ (in $2 \theta$ ) below the calculated $\mathrm{K} \alpha_{1}$ peak to $1^{\circ}$ above the $\mathrm{K} \alpha_{2}$ maximum. Background intensity was counted at each end of a scan range for a time equal to half the scan time. The intensities of three reflections in diverse regions of reciprocal space were recorded every 47 reflections to monitor crystal and instrument stability. Only small random fluctuations of these check reflections were observed during the course of data collection. The intensities of all lattice points for which $2 \theta<70^{\circ}$ were recorded.

For crystals 1 and 2, standard deviations were assigned to individual reflections by

$$
\sigma(I)=\left[\omega^{2}\left(\mathrm{CT}+B_{1}+B_{2}\right)+(p I)^{2}\right]^{1 / 2}
$$

where CT is the total integrated count, $B_{1}$ and $B_{2}$ are the background counts, and $I$ is the intensity. The value of $p=0.02$ was found to be appropriate for the instrumentation used. ${ }^{22}$ The intensities were corrected for Lorentz and polarization effects; the contribution of the monochromator crystal was calculated assuming it to be half-perfect and half-mosaic in character.

For crystal 3, reflections from two intensity-equivalent regions of reciprocal space ( $h k l, h \leq k \leq l ; h k l, k \leq l \leq h$ ) were similarly examined. The raw data from each region were corrected for Lorentz and polarization effects including that due to incident beam monochromatization; the reduced intensities were merged, and the resultant estimated standard deviations were assigned to each averaged reflection by the computer program COMPARE. ${ }^{23}$ Other details regarding data reduction have been discussed previously. ${ }^{24.25}$

Absorption corrections ( $\mu R \sim 0.35$ ) were judged to be negligible for all crystals. ${ }^{26}$ An empirical $\psi$ scan examination of crystal $3\left(\mathrm{Cs}_{12}-\right.$ $\mathrm{A} \cdot{ }^{1} / 2 \mathrm{Cs}$ ) showed only negligible fluctuations in intensity for three reflections. Only those reflections in each final data set for which the net count exceeded 3 times its standard deviation were used in structure solution and refinement. This amounted to 227,201 , and 360 reflections for crystals $1-3$, respectively.

## Structure Determination

$\mathrm{Cs}_{8.5} \mathrm{Na}_{3.5}-\mathbf{A} \cdot{ }^{1} /{ }_{2} \mathrm{Cs}$ (Crystal 1). Full-matrix least-squares refinement was initiated with the atomic parameters of the framework atoms $[(\mathrm{Si}, \mathrm{Al}), \mathrm{O}(1), \mathrm{O}(2)$, and $\mathrm{O}(3)]$ and $\mathrm{Cs}^{+}$ions at $\mathrm{Cs}(1), \mathrm{Cs}(2)$, and $\mathrm{Cs}(3)$ of $\mathrm{Cs}_{11} \mathrm{Ca}_{0.5}-\mathrm{A} \cdot{ }^{1} / 2 \mathrm{Cs} .{ }^{27}$ This model converged to $R_{1}=\sum\left|F_{o}-\right| F_{\mathrm{c}} \| / \sum F_{\mathrm{o}}=0.11$ and $R_{2}=\left(\sum w\left(F_{\mathrm{o}}\right.\right.$ $\left.\left.-\mid F_{\mathrm{c}}\right)^{2} / \sum w F_{0}^{2}\right)^{1 / 2}=0.10$ with occupancies of 3.08 (8), 4.31 (1), and 1.61 (8) for $\mathrm{Cs}(i), i=1-3$, respectively. These values suggested the presence of unreacted $\mathrm{Na}^{+}$ions at $\mathrm{Na}(1)$ on threefold axes. These were found on a Fourier function, and their inclusion reduced the error indices to $R_{1}=0.072$ and $R_{2}=0.060$. A subsequent Fourier function revealed some electron density at $\mathrm{Cs}(4)$, at $(0.32,0.32,0.5)$. Allowing all $\mathrm{Cs}(i)$ occupancies to vary except that at $\mathrm{Cs}(1)$, which was not permitted to exceed 3.0 (its maximum value by symmetry), and allowing all anisotropic thermal parameters to vary except for that at $\mathrm{Cs}(4)$, which was refined isotropically, led to $R_{1}=0.064$ and $R_{2}=0.043$, with converged occupancies given in the last column of Table Ia. The unusually large thermal parameter of $\operatorname{Cs}(4), 43$ (9) $\AA^{2}$, suggested that the $z$ coordinate of $\mathrm{Cs}(4)$ should be allowed to refine off the mirror plane at 0.5 . This was done, and in a refinement with all positional and thermal parameters free to vary, except that the

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Table I. Positional, Thermal, and Occupancy Parameters ${ }^{a}$ of $\mathrm{Cs}_{x} \mathrm{Na}_{12-x}-\mathrm{A} \cdot{ }^{1} / 2 \mathrm{Cs}, x=8.5$ or 12

${ }^{a}$ Positional and anisotropic thermal parameters are given $\times 10^{4}$. Numbers in parentheses are the estimated standard deviations in the units of the least significant figure given for the corresponding parameter. The anisotropic temperature factor is $\exp \left[-\left(\beta_{11} h^{2}+\beta_{22} k^{2}+\beta_{33} l^{2}+\beta_{12} h k+\beta_{13} h l+\right.\right.$ $\left.\left.\beta_{23} k l\right)\right]$. ${ }^{b}$ Rms displacements can be calculated from $\beta_{i i}$ values with the formula $\mu_{i}=0.225 a\left(\beta_{i j}\right)^{1 / 2}$, where $a=12.3 \AA$. ${ }^{\text {c }}$ Isotropic thermal parameter $\left(\AA^{2}\right)$. ${ }^{d}$ Occupancy factors are given as the number of ions per unit cell. ${ }^{\text {e }}$ Occupancy for $(\mathrm{Si})=12$; occupancy for $(\mathrm{Al})=12 .{ }^{f}$ Exactly ${ }^{1 / 2}$ by symmetry. ${ }^{g}$ This thermal parameter was fixed in least-squares refinement.
occupancies of all atoms and the isotropic thermal parameter of $\mathrm{Cs}(4)$ were fixed at the values given in Table Ia. $\mathrm{Cs}(4)$ refined to ( $0.33,0.33,0.46$ ) with $R_{1}=0.065$ and $R_{2}=0.052$. The final difference function was featureless except for some residual density near $\mathrm{Cs}(2)$ deep in the large cavity. See Table II.
The goodness-of-fit, $\left(\sum w\left(F_{0}-\left|F_{\mathrm{c}}\right|\right)^{2} /(m-s)\right)^{1 / 2}$, is 2.0 ; the number of observations, $m$, is 227 , and the number of parameters, $s$, is 33 . The final structural parameters and selected interatomic distances and angles are presented in Tables Ia and III, respectively.
$\mathrm{Cs}_{12}-\mathrm{A} \cdot{ }^{1} / 2 \mathrm{Cs}$ (Crystals 2 and 3). Full-matrix least-squares refinement of crystal 2 using the parameters of all framework atoms and $\mathrm{Cs}^{+}$ions in crystal 1 except $\mathrm{Cs}(4)$ quickly converged to $R_{1}=0.061$ and $R_{2}=0.051$. Refinement including $\mathrm{Cs}(4)$, which appeared on a subsequent difference function at ( $0.26,0.26,0.5$ ), with an isotropic thermal parameter lowered these to 0.054 and 0.040 , respectively, with occupancies of 2.99 (4), 7.01 (9), 2.18 (5), and 0.78 (12) for $\mathrm{Cs}(i), i=1-4$, and an unusually large thermal parameter for $\mathrm{Cs}(4)$. When the thermal parameter and occupancy of $\operatorname{Cs}(4)$ were free to vary, while all other occupancies were fixed at their nearest integers, they converged at $8(2) \AA^{2}$ and $0.55(7)$ with negligible changes in the error indices.

Least-squares refinement of crystal 3 yielded an unambiguous structure with occupancies of $3,7,2$, and 0.5 for the $\mathrm{Cs}(i)$ ions, $i=1-4$, resulting in the formula $\mathrm{Cs}_{12}-\mathrm{A} \cdot 1 / 2 \mathrm{Cs}$ with final error indices, $R_{1}=0.055$ and $R_{2}=0.042$. As had been seen in the refinement of the structure of crystal 2 , the inclusion of $\mathrm{Cs}(4)$ had a substantial effect on the error indices, reducing them by more than 0.01 . Least-squares refinement of this structure to convergence ( $R_{1}=0.053$ and $R_{2}=0.041$ ) in the lower space group Fm 3 c showed no change in the $\mathrm{Cs}^{+}$occupancies, indicating that they are not an artifact of the choice of space group. Table II contains final Pm3m Fourier information.

The values for the goodness-of-fit are 1.5 and 2.4 , the $m$ 's are 201 and 360 , and the $s$ 's are both 31 for crystals 2 and 3, re-

Table II. Highest Peaks on Two Final Fourier Functions ${ }^{a}$

| position | Fourier |  | diff Fourier |  |
| :---: | :---: | :---: | :---: | :---: |
|  | cryst 1 | cryst 3 | cryst 1 | cryst 3 |
| $\mathrm{Cs}(1)$ | 73.4 (5) | 81.4 (5) | 0.6 (5) | 2.2 (5) |
| $\mathrm{Cs}(2)$ | 57.6 (3) | $>99.9$ (3) ${ }^{\text {b }}$ | 1.0 (3) | 3.9 (3) |
| $\mathrm{Cs}(3)$ | 17.1 (3) | 20.2 (3) | 0.1 (3) | 0.0 (3) |
| $\mathrm{Cs}(4)$ | 3.8 (2) ${ }^{\text {c }}$ | 2.5 (2) ${ }^{\text {c }}$ | 0.2 (2) | 0.8 (2) |
| ca. $0.2,0.2,0.2$ | 12.9 (3) ${ }^{\text {d }}$ | 3.6 (3) ${ }^{e, f}$ | 1.0 (3) | 1.3 (3) |
| ca. $0.3,0.3,0.3^{8}$ | 4.4 (3) ${ }^{h}$ | 2.7 (1) ${ }^{i}$ | 1.1 (3) | 1.4 (1) |
| $0.5,0.5,0.5$ | 4.8 (8) |  | 1.1 (8) |  |

${ }^{a}$ Peak heights (e/ $\AA^{3}$ ). Esd's are given in parentheses. The esd at a general position is about $0.12 \mathrm{e} / \AA^{3}$ for all three crystals. ${ }^{b}$ The peak height is about $112 \mathrm{e} / \AA^{3}$. ${ }^{\text {c }}$ Although this peak was not high, its addition to least-squares lowered $R$ values appreciably and its occupancy remained significant. ${ }^{d} 0.2153,0.2153,0.2153$. ${ }^{\text {E }}$ Although this peak has moderate height, its occupancy refined to zero in least squares. It is midway between the high $\mathrm{Cs}(2)$ and $\mathrm{Cs}(3)$ peaks and may be attributed to termination-of-series error. Also, an ion at this position would be impossibly near (about $2.0 \AA$ ) a $\mathrm{Cs}^{+}$ion. fo.227, 0.227 , 0.227 . ${ }^{8}$ Very near $\mathrm{Cs}(2){ }^{h} 0.28,0.28,0.34 .^{i} 0.27,0.31,0.34$.
spectively. Their final structure parameters are presented in Table $\mathrm{Ib}, \mathrm{c}$.

All shifts in the final cycles of least-squares refinement for all three crystals were less than $0.1 \%$ of their corresponding standard deviations. Interactomic distances and angles are given in Table III.

For all structures, the full-matrix least-squares program used minimized $\sum w\left(F_{\mathrm{o}}-\left|F_{\mathrm{c}}\right|\right)^{2}$; the weight $w$ of an observation was the reciprocal square of $\sigma$, its standard deviation. Atomic scattering factors for $\mathrm{Cs}^{+}, \mathrm{Na}^{+}, \mathrm{O}^{-}$, and ( $\left.\mathrm{Si}, \mathrm{Al}\right)^{1.75+}$ were used. ${ }^{28,29}$

[^3]

Figure 1. Stereoview of a large cavity in $\mathrm{Cs}_{8} \mathrm{Na}_{4}-\mathrm{A}$. The zeolite A framework is drawn with heavy bonds between oxygen atoms and tetrahedrally coordinated ( $\mathrm{Si}, \mathrm{Al}$ ). Cation coordination by framework oxygens is indicated by fine lines. $\mathrm{Cs}^{+}$ions are relatively far from 6 -ring planes, while $\mathrm{Na}^{+}$ ions are almost at their centers. Ellipsoids of $20 \%$ probability are shown.


Figure 2. Stereoview of a large cavity in $\mathrm{Cs}_{9} \mathrm{Na}_{3}-\mathrm{A} \cdot \mathrm{Cs}$ (or $\mathrm{Cs}_{10} \mathrm{Na}_{3}-\mathrm{A}$ ). See the caption to Figure 1 for other details.

The function describing $(\mathrm{Si}, \mathrm{Al})^{1.75+}$ is the mean of the $\mathrm{Si}^{0}, \mathrm{Si}^{4+}$, $\mathrm{Al}{ }^{0}$, and $\mathrm{Al}^{3+}$ functions. All scattering factors were modified to account for the real component $\left(f^{\prime}\right)$ of the anomalous dispersion correction. ${ }^{30,31}$

## Crystallographic Results

In all three structures, $\mathrm{Cs}^{+}$ions are found at four crystallographic sites as summarized in Table IV. These structures differ only in the occupancies at $\mathrm{Cs}(2)$ and $\mathrm{Cs}(3)$, in the $z$ coordinate of $\mathrm{Cs}(4)$ opposite a 4-ring, and in the presence of unreacted $\mathrm{Na}^{+}$ ions in crystal 1.

In each structure, three $\mathrm{Cs}^{+}$ions at $\mathrm{Cs}(1)$ fill the equipoints of symmetry $C_{4 h}$ ( $D_{4 h}$ in $P m 3 m$ ) at the centers of the 8 -rings, as they have in all previously reported $\mathrm{Cs}^{+}$-exchanged zeolite A structures. ${ }^{4-10}$ Each $\mathrm{Cs}(1)$ cation is ca. 3.38 (1) $\AA$ from four $\mathrm{O}(1)$ oxygens and ca. 3.55 (1) $\AA$ from four O (2)'s (see interatomic distances in Table III). These distances are substantially longer than the sum of the ionic radii of $\mathrm{O}^{2-}$ and $\mathrm{Cs}^{+}, 2.99 \AA$. Theoretical calculations support this observation of a potential energy minimum at these positions. ${ }^{32,33}$
$\mathrm{Cs}_{8.5} \mathrm{Na}_{3.5}-\mathrm{A} \cdot{ }^{1 / 2} \mathrm{Cs}$. The structure of $\mathrm{Cs}_{8.5} \mathrm{Na}_{3.5}-\mathrm{A} \cdot{ }^{1} /{ }_{2} \mathrm{Cs}$ can perhaps best be viewed as having two kinds of $12.3-\AA$ "unit cells", of composition $\mathrm{Cs}_{8} \mathrm{Na}_{4}-\mathrm{A}$ and $\mathrm{Cs}_{9} \mathrm{Na}_{3}-\mathrm{A} \cdot \mathrm{Cs}$ (see Table IV for the distribution of $\mathrm{Cs}^{+}$ions in $\mathrm{Cs}_{8.5} \mathrm{Na}_{3.5}-\mathrm{A} \cdot 1 / 2 \mathrm{Cs}$ ). Possible atomic arrangements in the large cavities of $\mathrm{Cs}_{8} \mathrm{Na}_{4}-\mathrm{A}$ and $\mathrm{Cs}_{9} \mathrm{Na}_{3}-\mathrm{A} \cdot \mathrm{Cs}$ are shown in Figures 1 and 2, respectively. In $\mathrm{Cs}_{8} \mathrm{Na}_{4}-\mathrm{A}$, four unreacted $\mathrm{Na}^{+}$ions are placed tetrahedrally about the large cavity. Each $\mathrm{Na}^{+}$ion extends $0.58 \AA$ into the large cavity from the [111] plane at $\mathrm{O}(3)$ and coordinates to three $\mathrm{O}(3)$ oxygens at $2.33 \AA$. Three $\mathrm{Cs}^{+}$ions at $\mathrm{Cs}(2)$ are on threefold axes in the large cavity opposite 6 -rings. Each is 3.00 (1) $\AA$ from the three $\mathrm{O}(3)$ oxygens of its 6 -ring and $1.98 \AA$ from the [111] plane at $\mathrm{O}(3)$. A remaining 6 -ring is occupied by one $\mathrm{Cs}^{+}$ion at $\mathrm{Cs}(3)$ on a threefold axis in the sodalite unit. It is 3.05 (2) $\AA$ from three $\mathrm{O}(3)$ oxygens

[^4]Table III. Selected Interatomic Distances ( $\AA$ ) and Angles (deg) for $\mathrm{Cs}_{x} \mathrm{Na}_{12-x}-\mathrm{A} \cdot \frac{1}{2} \mathrm{Cs}, x=8.5$ or $12^{a}$

|  | $\begin{gathered} \hline \mathrm{Cs}_{8.5} \mathrm{Na}_{3.5} \\ \mathrm{~A} \cdot 1 / 2 \mathrm{Cs} \\ \text { (crystal } 1 \text { ) } \\ \hline \end{gathered}$ | $\begin{gathered} \mathrm{Cs}_{12}^{-} \\ \mathrm{A} \cdot 1 / 2 \mathrm{Cs} \\ \text { (crystal } 2 \text { ) } \\ \hline \end{gathered}$ | $\begin{gathered} \mathrm{Cs}_{12}^{-} \\ \mathrm{A}^{1} /{ }_{2} \mathrm{Cs} \\ \text { (crystal 3) } \\ \hline \end{gathered}$ |
| :---: | :---: | :---: | :---: |
| (Si, Al)-O(1) | 1.653 (6) | 1.656 (7) | 1.654 (4) |
| (Si, Al)-O(2) | 1.661 (5) | 1.658 (5) | 1.664 (3) |
| (Si, Al)-O(3) | 1.676 (4) | 1.670 (4) | 1.673 (2) |
| $\mathrm{Cs}(1)-\mathrm{O}(1)$ | 3.406 (14) | 3.369 (17) | 3.368 (10) |
| $\mathrm{Cs}(1)-\mathrm{O}(2)$ | 3.535 (17) | 3.570 (2) | 3.548 (9) |
| $\mathrm{Cs}(2)-\mathrm{O}(2)$ | 3.457 (3) | 3.422 (2) | 3.400 (1) |
| $\mathrm{Cs}(2)-\mathrm{O}(3)$ | 3.003 (10) | 2.991 (11) | 2.946 (6) |
| $\mathrm{Cs}(3)-\mathrm{O}(2)$ | 3.719 (19) | 3.422 (9) | 3.691 (10) |
| $\mathrm{Cs}(3)-\mathrm{O}(3)$ | 3.052 (15) | 3.045 (15) | 3.080 (9) |
| $\mathrm{Cs}(4)-\mathrm{O}(1)$ | 4.319 (72) | 3.382 (43) | 3.350 (43) |
| $\mathrm{Cs}(4)-\mathrm{O}(3)$ | 4.096 (85) | 3.382 (45) | 3.335 (44) |
| $\mathrm{Na}(1)-\mathrm{O}(3)$ | 2.330 (11) |  |  |
| $\mathrm{Cs}(1)-\mathrm{Cs}(2)$ | 5.122 (1) | 5.151 (1) | 5.161 (4) |
| $\mathrm{Cs}(1)-\mathrm{Cs}(4)$ | 4.586 (26) | 4.357 (5) | 4.353 (4) |
| $\mathrm{Cs}(2)-\mathrm{Cs}(2)$ | 5.356 (6) | 5.461 (4) | 5.513 (2) |
| $\mathrm{Cs}(2)-\mathrm{Cs}(3)$ | 4.034 (17) | 3.867 (15) | 3.868 (8) |
| $\mathrm{Cs}(3)-\mathrm{Cs}(3)$ | 3.875 (32) | 4.076 (30) | 3.978 (16) |
| $\mathrm{Cs}(3)-\mathrm{Cs}(4)$ | 6.171 (87) | 5.826 (31) | 5.849 (28) |
| $\mathrm{O}(1)-(\mathrm{Si}, \mathrm{Al})-\mathrm{O}(2)$ | 106.7 (8) | 106.9 (6) | 106.1 (5) |
| $\mathrm{O}(1)-(\mathrm{Si}, \mathrm{Al})-\mathrm{O}(3)$ | 112.0 (4) | 111.5 (5) | 111.4 (3) |
| $\mathrm{O}(2)-(\mathrm{Si}, \mathrm{Al})-\mathrm{O}(3)$ | 107.3 (4) | 108.2 (4) | 108.1 (3) |
| $\mathrm{O}(3)-(\mathrm{Si}-\mathrm{Al})-\mathrm{O}(3)$ | 111.2 (5) | 110.3 (6) | 111.5 (4) |
| (Si, Al)-O(1)-(Si, Al) | 146.4 (9) | 143.8 (11) | 143.7 (7) |
| (Si, Al)-O(2)-(Si, Al) | 157.1 (11) | 159.9 (4) | 158.6 (7) |
| $(\mathrm{Si}, \mathrm{Al})-\mathrm{O}(3)-(\mathrm{Si}, \mathrm{Al})$ | 142.3 (7) | 145.6 (8) | 144.7 (4) |
| $\mathrm{O}(3)-\mathrm{Cs}(2)-\mathrm{O}(3)$ | 81.2 (3) | 84.3 (3) | 85.5 (2) |
| $\mathrm{O}(3)-\mathrm{Cs}(3)-\mathrm{O}(3)$ | 79.7 (4) | 82.5 (4) | 81.0 (2) |
| $\mathrm{O}(3)-\mathrm{Na}(1)-\mathrm{O}(3)$ | 114.1 (5) |  |  |
| $\mathrm{Cs}(2)-\mathrm{Cs}(3)-\mathrm{Cs}(3)$ | 180.0 | 180.0 | 180.0 |

${ }^{a}$ The numbers in parentheses are the estimated standard deviations in the units of the least significant digit given for the corresponding parameter.
and is $2.05 \AA$ from its [111] plane at $\mathrm{O}(3)$. Another $\mathrm{Cs}^{+}$ion at $\mathrm{Cs}(4)$ is located opposite a 4 -ring, the usual position for the 12 th

Table IV. Distribution of $\mathrm{Cs}^{+}$Ions in Fully Dehydrated, Fully and Partially $\mathrm{Cs}^{+}$-Exchanged Zeolite A

| $\begin{gathered} \text { crystal } \\ \text { no. } \end{gathered}$ | overall formula: components | no. of $\mathrm{Cs}^{+}$ions |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | opposite 6 -rings in the |  | opposite$\text { 4-rings, } \mathrm{Cs}(4)$ | total |
|  |  | in 8-rings, $\mathrm{Cs}(1)$ | $\alpha$-cage, ${ }^{\text {a }}$ Cs $(2)$ | $\beta$-cage, ${ }^{\text {a }} \mathrm{Cs}(3)$ |  |  |
| 1 | $\mathrm{Cs}_{8.5} \mathrm{Na}_{3.5}$-A.1/2Cs: | 3 | 4 | 1.5 | $0.5{ }^{\text {b }}$ | 9 |
|  | $\mathrm{Cs}_{8} \mathrm{Na}_{4}-\mathrm{A}$ | 3 | 3 | 1 | $1^{\text {b }}$ | 8 |
|  | $\mathrm{Cs}_{9} \mathrm{Na}_{3}-\mathrm{A} \cdot \mathrm{Cs}$ | 3 | 5 | 2 | 0 | 10 |
| 2, 3 | $\mathrm{Cs}_{12}-\mathrm{A} \cdot 1 / 2 \mathrm{Cs}$ | 3 | 7 | 2 | 0.5 | 12.5 |
|  | $\mathrm{Cs}_{12}-\mathrm{A}$ | 3 | 6 | 2 | 1 | 12 |
|  | $\mathrm{Cs}_{12}$-A.Cs | 3 | 8 | 2 | 0 | 13 |

${ }^{a}$ The $\alpha$-cage is the large cavity. The $\beta$-cage is the sodalite unit. ${ }^{b}$ Nearly opposite a 4 -ring, at Wyckoff position 24 ( $m$ ).


Figure 3. Stereoview of a sodalite cavity in $\mathrm{Cs}_{12}-\mathbf{A}$. See the caption to Figure 1 for other details.


Figure 4. Stereoview of a large cavity in $\mathrm{Cs}_{12}-\mathrm{A}$. See the caption to Figure 1 for other details.


Figure 5. Stereoview of a sodalite cavity in $\mathrm{Cs}_{12}-\mathrm{A} \cdot \mathrm{Cs}\left(\right.$ or $\left.\mathrm{Cs}_{13}-\mathrm{A}\right)$. See the caption to Figure 1 for other details.
large monopositive ion. This $\mathrm{Cs}^{+}$ion is rather far from framework oxygens ( 4.10 (9) $\AA$ from O(3)) probably because of repulsive interaction with the $\mathrm{Na}^{+}$ion in an adjacent 6 -ring. (Also, less importantly, this distance may be virtual, a bit too long: This particular 4 -ring may have a distorted geometry due to the presence of its $\mathrm{Cs}^{+}$ion.) When this $\mathrm{Na}^{+}$is removed by further redox reaction, the 4 -ring $\mathrm{Cs}^{+}$ion can get closer to the framework, as shown in the unit cell of $\mathrm{Cs}_{12}$ - A (vide infra).

It is quite surprising to note, from their approach distances to framework oxygens, that all 13 cesiums and sodiums in the re-
maining half of the unit cells of $\mathrm{Cs}_{8.5} \mathrm{Na}_{3.5}-\mathrm{A} \cdot 1 / 2 \mathrm{Cs}$ appear to be cations: that is, $\mathrm{Cs}_{9} \mathrm{Na}_{3}-\mathrm{A} \cdot \mathrm{Cs}$ appears to be $\mathrm{Cs}_{10} \mathrm{Na}_{3}-\mathrm{A}$. With three $\mathrm{Na}^{+}$ions in 6 -rings, each unit cell contains seven $\mathrm{Cs}^{+}$ions located on the threefold axes: five in the large cavity and two in the sodalite unit opposite 6 -rings (see Table IV). The only way to place ten ions in the eight 6 -rings per unit cell is to have two such rings each accommodate two ions. Therefore, two rings are each occupied by two $\mathrm{Cs}^{+}$ions, one at $\mathrm{Cs}(2)$ and one at $\mathrm{Cs}(3)$, 4.03 (2) $\AA$ apart on the same threefold axis, one on each side of the 6 -ring. The second ion at $\mathrm{Cs}(3)$ (opposite a 6 -ring in the


Figure 6. Stereoview of a large cavity in $\mathrm{Cs}_{12}-\mathrm{A} \cdot \mathrm{Cs}$ (or $\mathrm{Cs}_{13}-\mathrm{A}$ ). See the caption to Figure 1 for other details.
sodalite unit) must be placed as far as possible from the first one to minimize their intercationic repulsive interaction; even so, it is only 3.88 (3) $\AA$ away. It follows, therefore, that all four $\mathrm{Cs}^{+}$ ions lie on the same threefold axis. These short inter-cesium distances describe isolated linear $\left(\mathrm{Cs}_{4}\right)^{3+}$ cations, $\mathrm{Cs}(2)$-Cs(3) $-\mathrm{Cs}(3)-\mathrm{Cs}(2)$ (vide infra).
$\mathrm{Cs}_{12}-\mathbf{A} \cdot{ }^{1} /{ }_{2} \mathrm{Cs}$. $\mathrm{Cs}^{+}$ions occupy four crystallographically distinct sites, as summarized in Table IV. The atomic arrangements in crystal 3, taken as representative, are shown in Figures 3-6. Crystal 2 has the same structure as crystal 3.

In addition to the three $\mathrm{Cs}^{+}$ions at the centers of the 8 -rings, each large cavity contains $7 \mathrm{Cs}^{+}$ions at $\mathrm{Cs}(2)$ and 0.5 at $\mathrm{Cs}(4)$. Each sodalite cage contains two $\mathrm{Cs}^{+}$ions at $\mathrm{Cs}(3)$ opposite 6 -rings. These are placed on the same threefold axis on opposite sides of the origin 4.08 (3) and 3.98 (2) $\AA$ apart, respectively, for crystals 2 and 3 . These short distances are exemplary of the ion crowding, which was anticipated for $\mathrm{Cs}-\mathrm{A} . \mathrm{Cs}_{12}-\mathrm{A} \cdot 1 / 2 \mathrm{Cs}$ may also best be discussed as having two kinds of $12.3-\AA$ unit cells, $\mathrm{Cs}_{12}-\mathrm{A}$ and $\mathrm{Cs}_{13}-\mathrm{A}$ in this case.

In $\mathrm{Cs}_{12}-\mathrm{A}$, two adjacent 6 -rings of each large cavity are occupied by sodalite unit $\mathrm{Cs}^{+}$ions, allowing one $\mathrm{Cs}^{+}$ion to be in the large cavity at $\mathrm{Cs}(4)$, opposite the 4 -ring that connects those two 6 -rings. Six large-cavity $\mathrm{Cs}^{+}$ions fill the remaining six 6 -rings. Each is 2.99 (1) $\AA$ from three $\mathrm{O}(3)$ oxygens and $1.89 \AA$ from the [111] plane at $\mathrm{O}(3)$ for crystal 2; these values are 2.95 (1) and $1.83 \AA$ for crystal 3. The large-cavity and sodalite-cavity views of $\mathrm{Cs}_{12}-\mathrm{A}$ are shown in Figures 3 and 4, respectively.

In $\mathrm{Cs}_{13}-\mathrm{A}$, all eight threefold axis sites in the large cavity are occupied by $\mathrm{Cs}^{+}$ions at $\mathrm{Cs}(2)$, so no 4 -ring sites are available. Again, the two $\mathrm{Cs}^{+}$ions in the sodalite unit must share a threefold axis with two of these eight $\mathrm{Cs}^{+}$ions at $\mathrm{Cs}(2)$ with inter-cesium distances of 3.87 (2) $\AA(\mathrm{Cs}(2)-\mathrm{Cs}(3))$ and 4.08 (3) $\AA(\mathrm{Cs}(3)-$ $\mathrm{Cs}(3)$ ) for crystal 2 and 3.87 (1) and 3.98 (2) $\AA$, respectively, for crystal 3. The large-cavity and sodalite-cavity views are presented in Figures 5 and 6, respectively.

If the electrons of the extra cesium atoms are viewed as being delocalized only among the closest $\mathrm{Cs}^{+}$ions, one may recognize isolated linear cesium clusters, $\left(\mathrm{Cs}_{4}\right)^{3+}, \mathrm{Cs}(2)-\mathrm{Cs}(3)-\mathrm{Cs}(3)-\mathrm{Cs}(2)$ (Figure 7)

Cesium reacts with dehydrated $\mathrm{Ca}_{6}-\mathrm{A}$ and $\mathrm{K}_{12}-\mathrm{A}$ to give the same (or nearly the same) product, $\mathrm{Cs}_{12}-\mathrm{A} \cdot{ }^{1} / 2 \mathrm{Cs}$. Crystals of intermediate composition were also prepared from $\mathrm{Ca}_{6}-\mathrm{A}$ as in this work. With less certainty, $\mathrm{Co}_{4} \mathrm{Na}_{4}-\mathrm{A}$ appears to react to give $\mathrm{Cs}_{12}-\mathrm{A} \cdot 1 / 2 \mathrm{Cs}$ also. These results ${ }^{27}$ will be presented in subsequent reports.

## Discussion

Fully $\mathrm{Cs}^{+}$-exchanged, fully dehydrated zeolite $\mathrm{A}, \mathrm{Cs}_{12}-\mathrm{A} \cdot 1 / 2 \mathrm{Cs}$, has been synthesized by the reduction of the $\mathrm{Na}^{+}$ions in $\mathrm{Na}_{12}-\mathrm{A}$ with ca. 0.1 Torr of cesium vapor at $350^{\circ} \mathrm{C}$. The intermediate composition $\mathrm{Cs}_{8.5} \mathrm{Na}_{3.5}-\mathrm{A} \cdot{ }^{1} /{ }_{2} \mathrm{Cs}$ formed upon reaction at $250^{\circ} \mathrm{C}$.

In the crystal structures of $\mathrm{Cs}_{x} \mathrm{Na}_{12-x}-\mathrm{A} \cdot{ }^{1} / 2 \mathrm{Cs}$, whether $x$ is 8.5 or $12,0.5$ extra cesium was found per unit cell. Each of these atoms associates with three $\mathrm{Cs}^{+}$ions to form $\left(\mathrm{Cs}_{4}\right)^{3+}$ (see Figure 7). The condensation of three $\mathrm{Cs}^{+}$ions into a relatively small volume of space, as the cesium atom involved allows, apparently


Figure 7. Linear cesium cluster, $\left(\mathrm{Cs}_{4}\right)^{3+}$, on a threefold axis passing through the sodalite cavities of $\mathrm{Cs}_{9} \mathrm{Na}_{3}-\mathrm{A} \cdot \mathrm{Cs}$ and $\mathrm{Cs}_{12}-\mathrm{A} \cdot \mathrm{Cs}$. Bond lengths are in angstroms. Ellipsoids of $20 \%$ probability are shown.
leads to a lowering of the net electrostatic repulsive energy among the cesium species as compared to that in $\mathrm{Cs}_{8.5} \mathrm{Na}_{3.5}-\mathrm{A}$ and in $\mathrm{Cs}_{12}-\mathrm{A}$. In addition, some covalent bonding has been introduced among the cesiums. The extra cesium atoms found in $\left(\mathrm{Cs}_{4}\right)^{3+}$ of $\mathrm{Cs}_{8.5} \mathrm{Na}_{3.5}-\mathrm{A} \cdot{ }^{1} /{ }_{2} \mathrm{Cs}$ indicate that full $\mathrm{Cs}^{+}$-exchange is not required for extra cesium to be sorbed. Rather, it is at some intermediate level of exchange that the concentration of $\mathrm{Cs}^{+}$ions and the degree of ion-crowding is sufficient to cause the zeolite to sorb extra Cs atoms.

Alternatively, $\mathrm{Cs}_{12}-\mathrm{A} \cdot{ }^{1} /{ }_{2} \mathrm{Cs}$ and $\mathrm{Cs}_{8.5} \mathrm{Na}_{3.5}-\mathrm{A} \cdot{ }^{1} /{ }_{2} \mathrm{Cs}$ may be viewed as materials with 12.5 ions and 0.5 excess electron per unit cell. The $\mathrm{Cs}^{+}$ions in $\mathrm{Cs}_{12}-\mathrm{A} \cdot{ }^{1} / 2 \mathrm{Cs}$ form a three-dimensional array with inter-cesium distances of 3.87 (1), 3.98 (2), 4.35 (1), 5.16 (1), and 5.51 (1) $\AA$ for $\mathrm{Cs}(2)-\mathrm{Cs}(3), \mathrm{Cs}(3)-\mathrm{Cs}(3), \mathrm{Cs}(1)-\mathrm{Cs}(4)$, $\mathrm{Cs}(1)-\mathrm{Cs}(2)$, and $\mathrm{Cs}(2)-\mathrm{Cs}(2)$, respectively (distances from the structure of crystal 3). These are shorter than or comparable to those in Cs metal $(5.31 \AA)$. ${ }^{34}$ Therefore, the excess electrons may form a metallic continuum of electron density, encompassing the entire volume of the single crystal of zeolite $A$. To test this alternative, a freshly prepared powdered sample of $\mathrm{Cs}_{12}-\mathrm{A} \cdot{ }^{1} / 2 \mathrm{Cs}$ was examined within its Pyrex container under vacuum. The sample was placed in the field of an oscillating circuit; the simple instrument used is sometimes called a metal detector or a grip dip meter. The eddy currents, which would be induced in a metal, would drain energy from this field. In a wide range of frequency, no noticeable energy loss was detected with $\mathrm{Cs}_{12}-\mathrm{A} \cdot 1 / 2 \mathrm{Cs}$, although positive results were achieved with powders of aluminum or graphite. This suggests that the excess electrons are localized among the closest $\mathrm{Cs}^{+}$ions, those of the $\left(\mathrm{Cs}_{4}\right)^{3+}$ clusters.

It appears that the intermediate product $\mathrm{Cs}_{8.5} \mathrm{Na}_{3.5}-\mathrm{A} \cdot{ }^{1} /{ }_{2} \mathrm{Cs}$ is the result of incomplete reaction due to slow diffusion kinetics within the zeolite at $250^{\circ} \mathrm{C}$; it seems unlikely that a temperature difference of only $100^{\circ} \mathrm{C}$ would cause this mixed-ion composition to be the thermodynamically stable one. Nonetheless, note that $\mathrm{Na}^{+}$ions and Cs atoms coexist within this crystal. That they have not reacted indicates that the chemical activity of the Cs atoms are diminished by their incorporation into $\left(\mathrm{Cs}_{4}\right)^{3+}$ clusters.
The $\left(\mathrm{Cs}_{4}\right)^{3+}$ cluster can be considered to be a one-dimensional particle-in-a-box system of four linearly arranged $\mathrm{Cs}^{+}$ions with
(34) Interatomic Distances, Supplement; The Chemical Society: London, 1965; p S-5s.
one electron delocalized among them. The length of this box, 15.4 $\AA$, is approximated by the sum of the three bond lengths plus twice the ionic radius of $\mathrm{Cs}^{+}$. A broad absorptive transition ( $1 \rightarrow 4$ ) is allowed near the middle of the visible range at about $5220 \AA$, which could account for the black color of the $\left(\mathrm{Cs}_{4}\right)^{3+}$-containing crystals.

At $350^{\circ} \mathrm{C}$, all $\mathrm{Na}^{+}$ions in $\mathrm{Na}_{12}$-A were reduced and replaced by $\mathrm{Cs}^{+}$ions; this solvent-free ion-exchange reaction went to completion. Simultaneously, no evidence for reaction with the zeolite framework was observed at the temperatures used in this work. This is consistent with the highly positive values of $\Delta G^{\circ}$ for the reactions of $\mathrm{Al}_{2} \mathrm{O}_{3}$ or $\mathrm{SiO}_{2}$ with cesium and is verified experimentally by the very strong diffraction pattern of the resulting zeolite crystal. It is further indicated by the observation that the colorless appearance of the crystal can be restored simply by exposure to the atmosphere; particles of Al or Si , if they had been generated and were responsible for the black color of the crystal, would probably not be easily oxidized.

Several additional experimental observations have been made. When crystals of $\mathrm{Cs}_{12}-\mathrm{A} \cdot{ }^{1} / 2 \mathrm{Cs}$ were maintained under vacuum at a temperature above $650^{\circ} \mathrm{C}$, a colorless transparent layer developed very slowly to a thickness of ca. $5 \mu \mathrm{~m}$. Even after the crystal was heated at $850^{\circ} \mathrm{C}$ for 2 days, the black interior of the crystal was still seen without noticeable change in the thickness of the transparent layer. This could indicate that $\mathrm{Cs}_{12}-\mathrm{A} \cdot{ }^{1} / 2 \mathrm{Cs}$ decomposes to transparent crystalline $\mathrm{Cs}_{12}-\mathrm{A}$ by losing its extra cesium atoms. Heating to $1000^{\circ} \mathrm{C}$ confirms this; all of the excess cesium atoms are lost, yielding $\mathrm{Cs}_{12}-\mathrm{A}$ (with three, seven, and two $\mathrm{Cs}^{+}$ions at $\mathrm{Cs}(i), i=1-3$, respectively), which is colorless as expected. These topics will be presented in a subsequent report. ${ }^{35}$
$\mathrm{Cs}_{12}$ - A is remarkably stable. $\mathrm{Na}_{12}-\mathrm{A}$ is stable only to about $750^{\circ} \mathrm{C}$ in air ${ }^{36}$ or under vacuum. Stabilities up to about $825^{\circ} \mathrm{C}$ are found in $\mathrm{K}_{12}-\mathrm{A}$ and in nearly fully $\mathrm{Ca}^{2+}$-exchanged zeolite A. ${ }^{36}$

After the crystal was heated at $650^{\circ} \mathrm{C}$ for 7 days, the interior of the crystal became dark green. This may indicate that some small amount of the green sub-oxide $\mathrm{Cs}_{3} \mathrm{O}^{37}$ had formed. Note that the uptake of excess $\mathrm{Cs}^{0}$ by $\mathrm{Cs}_{2} \mathrm{O}$ to form $\mathrm{Cs}_{3} \mathrm{O}$ is like that by $\mathrm{Cs}_{8.5} \mathrm{Na}_{3.5}-\mathrm{A}$ and $\mathrm{Cs}_{12}-\mathrm{A}$ to form $\left(\mathrm{Cs}_{4}\right)^{3+}$-containing zeolites A. $\mathrm{Cs}_{2} \mathrm{O}^{38}$ must also be considered a cationally crowded material.
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It has also been observed that, upon exposure to the atmosphere, the black $\mathrm{Cs}_{12}-\mathrm{A} \cdot{ }^{1} / 2 \mathrm{Cs}$ crystal became colorless along a welldefined retreating front over a period of 2 weeks as the atmosphere slowly diffused into an $80-\mu \mathrm{m}$ crystal. This may be ascribed to a reaction between the excess cesium within the crystal and water or oxygen diffusing into the crystal from the surface, to produce colorless cesium hydroxide (and hydrogen) or cesium oxide, respectively.
Recent ${ }^{29}$ Si MAS NMR work ${ }^{39}$ indicates that the zeolite A framework contains about 3 or $4 \%$ more Si than Al . If that is true, the crystallographic results reported here would need to be interpreted somewhat differently. Unit cells of composition $\mathrm{Cs}_{11} \mathrm{Si}_{13} \mathrm{Al}_{11} \mathrm{O}_{48}$ and $\mathrm{Cs}_{12} \mathrm{Si}_{12} \mathrm{Al}_{12} \mathrm{O}_{48}$ would need to be considered for crystals 2 and 3 (for example) prior to cesium atom absorption. $\mathrm{Cs}_{12} \mathrm{Si}_{12} \mathrm{Al}_{12} \mathrm{O}_{48}$ would certainly have sorbed a full cesium atom per unit cell to give $\mathrm{Cs}_{12} \mathrm{Si}_{12} \mathrm{Al}_{12} \mathrm{O}_{48}$. Cs , but the present crystallographic results are only marginally consistent at best with the proposition either that $\mathrm{Cs}_{11} \mathrm{Si}_{13} \mathrm{Al}_{11} \mathrm{O}_{48}$ would sorb a cesium atom or that it would not. (If it did, only $\left(\mathrm{Cs}_{2}\right)^{+}$clusters like that shown in Figure 3 could exist in sodalite units of this composition due to packing considerations.) (Such an analysis might resolve a difficult point in the present interpretation: $\mathrm{Cs}_{12} \mathrm{Si}_{12} \mathrm{Al}_{12} \mathrm{O}_{48}$ sorbs only $0.5 \mathrm{Cs}^{0}$ per unit cell; if half of the unit cells sorb $\mathrm{Cs}^{0}$, we must ask why the remaining half does not. Various kinetic or equilibrium (packing) arguments might be proposed.) In recent work awaiting publication, $\mathrm{Cs}_{12}-\mathrm{A} \cdot 3 / 4 \mathrm{Cs}$ appears to be the composition of a product, and this could, but need not be, interpreted to give the composition indicated by Blackwell et al. ${ }^{39}$ However, the packing constraint on the occupancies, $G_{\mathrm{Cs}(2)}+2 G_{\mathrm{Cs}(4)} \leq 8$ for crystals 2 and 3, does not allow the present composition to be interpreted as $\mathrm{Cs}_{12}-\mathrm{A} \cdot{ }^{3} / 4 \mathrm{Cs}$. In any event, half or more of the unit cells in $\mathrm{Cs}_{12}-\mathrm{A}^{1} \cdot 1 / 2 \mathrm{Cs}$ are of composition $\mathrm{Cs}_{12} \mathrm{Si}_{12} \mathrm{Al}_{12} \mathrm{O}_{48} \cdot \mathrm{Cs}$, and each contains a linear $\left(\mathrm{Cs}_{4}\right)^{3+}$ cluster. The remainder may be $\mathrm{Cs}_{12} \mathrm{Si}_{12} \mathrm{Al}_{12} \mathrm{O}_{48}, \mathrm{Cs}_{11} \mathrm{Si}_{13} \mathrm{Al}_{11} \mathrm{O}_{48}$, or $\left(\mathrm{Cs}_{2}\right)^{+}$-containing $\mathrm{Cs}_{12^{-}}$ $\mathrm{Si}_{13} \mathrm{Al}_{11} \mathrm{O}_{48}$.

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Registry No. Cs, 7440-46-2; $\mathrm{NaSiAlO}_{4}, 12003-51-9 ; \mathrm{Cs}_{12}-\mathrm{A}, 12003-$ $48-4 ; \mathrm{Cs}_{8} \mathrm{Na}_{4}-\mathrm{A}, 110826-62-5 ; \mathrm{Cs}_{9} \mathrm{Na}_{3}-\mathrm{A} \cdot \mathrm{Cs}, 110874-05-0 ; \mathrm{Cs}_{12}-\mathrm{A} \cdot \mathrm{Cs}$, 110903-50-9.

Supplementary Material Available: Table of observed and calculated structure factors for fully dehydrated, fully or partially $\mathrm{Cs}^{+}$-exchanged zeolite $\mathrm{A}, \mathrm{Cs}_{x} \mathrm{Na}_{12-x}-\mathrm{A} \cdot{ }^{1} / 2 \mathrm{Cs}, x=8.5$ or 12 (7 pages). Ordering information is given on any current masthead page.

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